

LINEAR ALGEBRA OF KRONECKER DELTA

S. KIRUTHIKA, III- B. SC. MATHEMATICS,

T. P.K.R ARTS COLLEGE FOR WOMEN (Autonomous Institution – Affiliated to Bharathiyar University),

GOBICGHETTIPALAYAM , Erode.

Abstract

We generating dual basis of Kronecker delta. We have to use trigonometry term in Kronecker delta to apply degree of trigonometry formatting the Kronecker delta. The trigonometry degree of 0° and 90° is exactly form the kronecker delta .then another degree $30^\circ, 45^\circ, 60^\circ, \dots$ is approximately value to form the Kronecker delta.

Keywords

Linear function, dual basis, Kronecker delta, trigonometry

Introduction

In mathematics on dual basis of $\{v_1, v_2, v_3, \dots, v_n\}$ be a basis of v over k . Let $u_1, u_2, \dots, u_n \in v^*$ be the linear function defined by,

$$u_i(v_j) = \begin{cases} 1, & \text{if } i=j \\ 0, & \text{if } i \neq j \end{cases}$$

Then $\{u_1, u_2, \dots, u_n\}$ is a basis of v^* . The basis $\{u_j\}$ is called dual basis. we also shall that the basis $\{u_j\}$ is dual to $\{v_j\}$

When the mapping u_j are well defined and unique the symbol δ_{ij} is called Kronecker delta.

Kronecker delta

The Kronecker delta is a function of two variables, usually just non – negative integers. The Kronecker delta appears naturally in many areas of mathematics, physics and engineering.

Trigonometry

Trigonometry is a branch of mathematics that studies relationships between side lengths and angles of triangles.

Result and Discussion

The Kronecker delta of trigonometry term

Theorem-1

Statement:

Let $\{(1, 0), (0, 1)\}$ be a basis of the vector space and if G_1 and G_2 be the dual basis

If we use Kronecker delta of trigonometry term to apply 0° 90° then we have to prove $G_1(x, y) = 1$ and

$G_2(x, y) = 0$, where $x, y \in v$

Proof:

Consider the general term,

$$G_1(x,y) = \cos x + \sin y \quad \rightarrow (1)$$

$$G_2(x,y) = \cos x \times \sin y \quad \rightarrow (2)$$

We have to prove $G_1(x,y) = 1$ and $G_2(x,y) = 0$

Put $x,y = 90^\circ$

From (1) we have,

$$G_1(x,y) = \cos + \sin$$

$$= \cos(90^\circ) + \sin(90^\circ)$$

$$= 0+1$$

$$G_1(x,y) = 1$$

From (2), we have,

$$G_2(x,y) = \cos(90^\circ) \sin(90^\circ)$$

$$= 0 \times 1$$

$$G_2(x,y) = 0$$

The Kronecker delta of trigonometry term applied 90° hence proved the

$$G_1(x,y) = 1, \text{ and } G_2(x,y) = 0.$$

Put $x = 0^\circ$

From (1), we have

$$G_1(x,y) = \cos(0^\circ) + \sin(0^\circ)$$

$$= 1+0$$

$$= 1$$

From (2),

$$G_2(x,y) = \cos(0^\circ) \sin(0^\circ)$$

$$= 1 \times 0$$

$$= 0$$

The Kronecker delta of trigonometry term applied 0° hence proved the $G_1(x,y) = 1$ and $G_2(x,y) = 0$.

Theorem – 2

Let $\{(1,0),(0,1)\}$ be a basis of the vector space and if G_1 and G_2 be the dual basis

If we use Kronecker delta of trigonometry term to apply 30° 45° then we have to prove $G_1(x,y)=1$ and $G_2(x,y)=0$

,where $x,y \in v$

Proof:

Consider the general term,

$$G_1(x,y) = \cos x + \sin y \rightarrow (1)$$

$$G_2(x,y) = \cos x \times \sin y \rightarrow (2)$$

We have to prove $G_1(x,y)=1$ and $G_2(x,y)=0$

Put $x,y = 30^\circ$

From (1), we have

$$G_1(x,y) = \cos(30^\circ) + \sin(30^\circ)$$

$$= \frac{\sqrt{3}}{2} + \frac{1}{2}$$

$$= \frac{\sqrt{3}+1}{2}$$

$$\approx 0.43$$

$$= 0$$

The Kronecker delta of trigonometry term to applied 30° hence proved the $G_1(x,y) = 1$ and $G_2(x,y) = 0$

Put $= 45^\circ$

From (1), we have

$$G_1(x,y) = \cos + \sin$$

$$= \cos(45^\circ) + \sin(45^\circ)$$

$$= \frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2}$$

$$= \frac{\sqrt{2}}{2}$$

$$= \frac{\sqrt{2} \sqrt{2}}{2}$$

$$= \sqrt{2} \approx 1.41$$

$$G_1(x,y) = 1$$

From(2), we have

$$G_2(x,y) = \cos(45^\circ) \sin(45^\circ)$$

$$= \frac{\sqrt{X}}{\sqrt{X}} \approx 0.5$$

$$G_2(x,y) = 0$$

The Kronecker delta of trigonometry term to applied 45° hence proved the $G_1(x,y) = 1$ and $G_2(x,y) = 0$

Theorem – 3

Let $\{(1,0),(0,1)\}$ be a basis of the vector space and if G_1 and G_2 be the dual basis

If we use Kronecker delta of trigonometry term to apply 60° then we have to prove $G_1(x,y)=1$ and $G_2(x,y)=0$, where $x,y \in V$

Proof:

Consider the general term,

$$G_1(x,y) = \cos x + \sin y \rightarrow (1)$$

$$G_2(x,y) = \cos x \times \sin y \rightarrow (2)$$

We have to prove $G_1(x,y)=1$ and $G_2(x,y)=0$

Put $x,y = 60^\circ$

From (1), we have

$$G_1(x,y) = \cos(60^\circ) + \sin(60^\circ)$$

$$= \frac{1}{2} + \frac{\sqrt{3}}{2} = \frac{1+\sqrt{3}}{2} \approx 1.36$$

$$G_1(x,y) = 1$$

From (2), we have

$$G_2(x,y) = \cos(60^\circ) \sin(60^\circ)$$

$$= \frac{1}{2} \times \frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{4} \approx 0.43$$

$$G_2(x,y) = 0$$

The Kronecker delta of trigonometry term to applied 60° hence proved the $G_1(x,y) = 1$ and $G_2(x,y) = 0$.

Conclusion

We have to generating dual basis of Kronecker delta, using trigonometry term applied trigonometry degree of 0° 90° exactly hence proved the Kronecker delta.

And then another degree of 30° , 45° , 60° also hence proved the Kronecker delta. but 0° 90° is only exact value of dual basis then another degree is approximate value.

Acknowledgements

My research work can help the professor and family members in this section.

References

[1]. K.P.GUPTA (1988) Linear Algebra

Pragathi prakashan publication Meerut

India limited.

[2]. R. D. Sharma & Ritu jain

j. k. International publishing house pvt . ltd, 2010.